In this tutorial, we will learn the basics of performing motion analysis using COSMOSMotion. Although the tutorial can be completed by anyone with a basic knowledge of SolidWorks parts and assemblies, we have provided enough detail so that students with an understanding of the physics of mechanics will be able to relate the results to those obtained by hand calculations.

Begin by creating the six part models detailed on page 2. For each part, define the material by right-clicking "Material" in the FeatureManager and selecting "Edit Material." The Materials Editor will appear, as shown here. Select "Alloy Steel" from the list of steels in the SolidWorks materials library. The part will appear with the material color (gray) stored in the library for steel. If you prefer to show the part with a color that you have defined, uncheck the "Use material color" box. Click the check mark to apply the material.

#### Rotation of a Wheel

To begin, we will analyze a simple model of a wheel subjected to a torque. From Newton's Second Law, we know that the sum of the forces acting on a body equals the mass of the body times the acceleration of the body, or

$$\sum F = ma$$

The above equation applies to bodies undergoing linear acceleration. For rotating bodies, Newton's Second Law can be written as:

$$\sum M = I\alpha$$

Where  $\sum M$  is the sum of the moments about a point in the body, I is the mass moment of inertia of the body, and  $\alpha$  is the angular acceleration of the body. The moment of inertia about an axis is defined as:

$$I = \int mr^2 dV$$

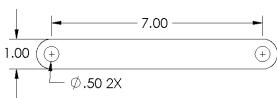
where r is the radial distance from the axis. For simple shapes, the moment inertia is easy to calculate. However, for more complex components, calculation of I can be difficult. SolidWorks allows mass properties, including moments of inertia, to be determined easily.

# Open the part "Wheel." From the main menu, select "Mass Properties."

The mass properties of the wheel are reported in the pop-up box. For this part, the mass is 40.02 pounds-mass, and the moment of inertia about the z-axis is 609.3 lb<sub>m</sub>in<sup>2</sup>. Note that if you centered the part about the origin, then the properties, labeled "Taken at the center of mass and aligned with the output coordinate system" will be identical to those labeled "Taken at the center of mass."

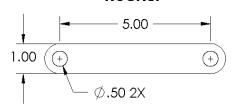


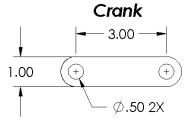
#### Frame



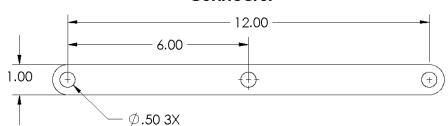
Thickness of all links = 0.25 All dimensions are inches

#### Rocker

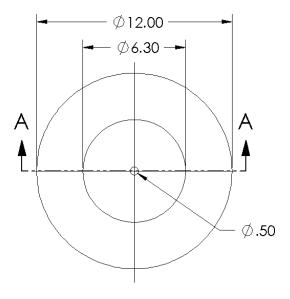




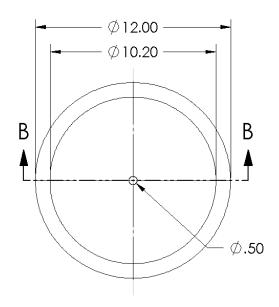
#### Connector

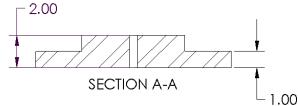


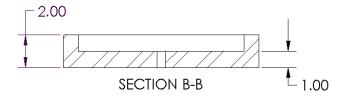
#### Wheel



#### Wheel2



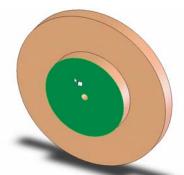




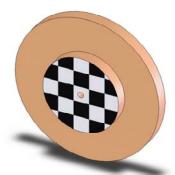
All dimensions are inches

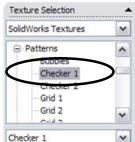
Since the wheel is symmetric about the axis of rotation, it will be difficult to visualize the rotational motion in the model. Adding a non-symmetric pattern to one of the faces of the wheel will be helpful.

Select the face shown here. Click on the Textures Tool, and select a texture. The "Checker 1" texture from the "Patterns" group is a good choice. Move the scale slider bar under the preview window to make the pattern larger or smaller, as desired. Click the check mark to apply the pattern to the face.



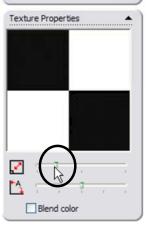






Save the part file. Open the part "Wheel2." Find the mass properties, and apply a texture to a face of the model. Save the part file.





Note that the mass of this part  $(40.14 \text{ lb}_m)$  is almost identical to that of the other wheel, but the mass moment of inertia  $(837.0 \text{ lb}_m \text{in}^2)$  is about 37% greater. The mass moment of the part depends not only on the part's mass, but also on how that mass is distributed. As more mass is placed further away from the axis of the part, then the mass moment of inertia about that axis increases (note the "r<sup>2</sup>" in the equation on page 1).

#### Open a new assembly. Insert the component "Frame."

Since the first component inserted into an assembly is fixed, it is logical to insert the component representing the stationary component (the "frame" or "ground" component) first.

Activate the COSMOSMotion program by selecting Tools: Add-Ins from the main menu. Select COSMOSMotion from the menu of available add-ins and click OK.



With COSMOSMotion activated, a "Motion" menu will be added to the main menu. Also, a tab to the motion model will appear above the FeatureManager.

#### Click the Motion icon above the FeatureManager.

A pop-up box will appear, asking if you would like to add the existing parts to Grounded or Moving Parts.

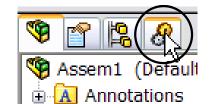
Click Yes to add the frame link as a grounded (stationary) part in the motion model.

Notice that the frame part is listed under "Ground Parts" in the motion model manager.

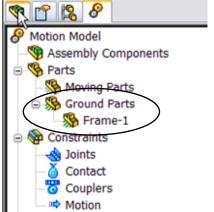
You can switch back to the modeling environment by clicking on the FeatureManager icon. However, you can perform modeling functions (adding components, adding mates,

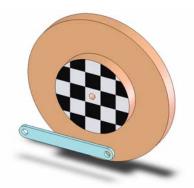
etc.) while in the motion model environment.











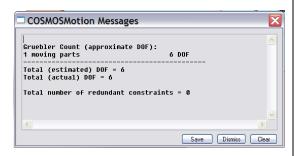
Insert the part "Wheel" into the assembly. Click Yes to add the part to the motion model.



From the menu, select Motion: Show Simulation Panel.



Click on the Calculate button. A pop-up box will appear as shown here.

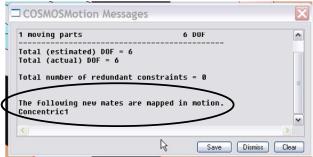


The box that appears shows an analysis of the model. Each moving part has six *degrees of freedom* in 3-D space. The part can translate along the x, y, and z axes, and can rotate about the x, y, and z axes. Since we have one moving part (the wheel), and its motion is so far unconstrained, the number of degrees of freedom is six.

Click Dismiss to close the message box. Select the Mate Tool. Add a concentric mate between the center hole of the wheel and and one of the holes in the frame link. Be sure to select the cylindrical faces for the mate and not edges.

A message box will appear, informing you that a concentric joint has been created based on the mate.

#### Click Dismiss to close the message box.



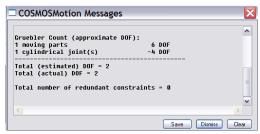
A concentric joint

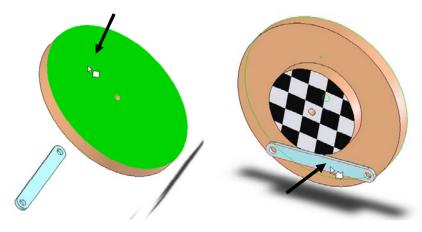
has been added. By zooming in on the joint area, you can see the joint illustrated (shown here with the model in wireframe mode for clarity). Each joint restricts degrees of freedom. The cylindrical joint prevents translation in the x and y directions, and also prevents rotations about the x and y axes. Therefore, two degrees of freedom (DOF) remain: the wheel can turn about the z axis and can also translate along the z axis.

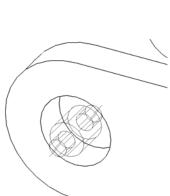
# In the Simulation Panel, click the Calculate button.

The message box confirms that two degrees of freedom remain in the model.

Add a coincident mate between the back face of the wheel and the front face of the frame link.







Dismiss the message box confirming the creation of a joint from the mate. Click the Calculate button in the Simulation panel.

The message box now shows that the joint has been changed into a revolute joint. A revolute joint allows only one degree of freedom. It is represented by a hinge icon.

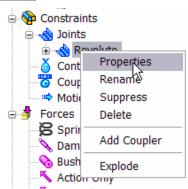




#### Close the Mate Command window, and dismiss the message box.

We will now apply a prescribed rotational motion to the revolute joint, and determine the torque required to produce the motion.

Right-click the Revolute joint under Joints in the Motion Model Manager. Select Properties.



Edit Mate-Defined Joint

Motion Friction FEA Properties

Initial Velocity: 0

Motion On: Rotate Z

**Choose the motion type as Acceleration.** (The "Motion On" will be set to Rotate Z, with no other choices available, since that is the only motion allowed by the revolute joint.)

Set the type of acceleration as constant, and the value as  $600 \text{ deg/s}^2$ .

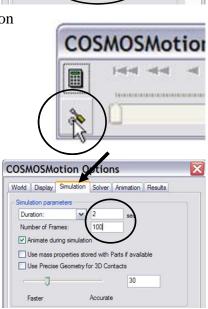
Note that if you calculate the number of DOF, it is now zero, as the only unconstrained motion now is being "driven" by the prescribed motion added to the joint.

**Click the Simulation Settings icon in the Simulation Panel.** 

Under the Simulation tab, set the duration to 2 seconds and the number of frames to 100.

Run the simulation by clicking the calculator on the Simulation Panel.





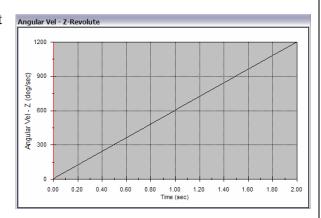
Right-click the Revolute joint in the Motion Model Manager. Choose Plot: Angular Velocity: Z Component.

Note that when you right-click on the joint, a different menu appears than before. After a simulation has been performed, the menus allow you to display results. If you want Constraints 🚊 📣 Joints 🕁 🚷 🎮 Angular Acceleration Con Angular Velocity X Component Cou Add Angular Displacement Power Consumption Y Component Motion Projection Angles Z Gomponent Springs Magnitude Reaction Force Dampers Reaction Moment Bushings Rotary Motion Generator Action Only ∆ction/Poaction

to change the parameters of the simulation, then you must first delete the results of the last simulation.

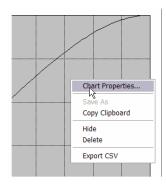
A plot of the angular velocity is displayed. Since we specified a constant acceleration, the velocity change is linear. The final velocity after 2 seconds is:

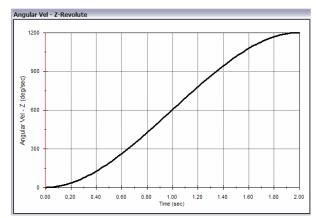
$$\omega = \alpha t = \left(600 \frac{\text{deg}}{\text{s}^2}\right) (2 \text{ s}) = 1200 \frac{\text{deg}}{\text{s}}$$



The appearance of the plot can be changed with commands similar to those for spreadsheet graphs. For example, the background color can be changed by right-clicking in the graph are and selecting Chart Properties. The appearance of the line (color/weight) can be changed by right-clicking on the curve and selecting Curve properties.

Make any desired changes to the appearance of the plot.

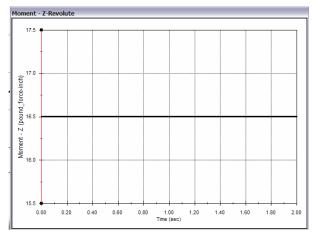




We will now plot the value of the torque that is desired to drive the wheel at the specified motion.

Right-click the Revolute joint in the Motion Model Manager. Choose Plot: Rotary Motion Generator: Moment Z. Modify the appearance of the chart as desired.

The plot created shows a constant value of torque.

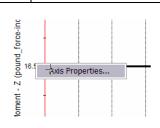


Introduction to Solid Modeling Using SolidWorks 2006

**COSMOSMotion Tutorial** 

Page 8

Right-click on the y-axis and select Axis Properties. Under the Numbers tab, change the number of decimal places to 2.



The torque required to produce the motion is seen to be 16.53 in·lb.

We can check this result by applying the equation

pplying the eq
$$\sum M = I\alpha$$

Moment - Z (pound\_force-inch) 16.53

Delete the simulation results by clicking on the calculator icon in the Simulation Panel. Right-click on the part name (Wheel) and select Properties.

Since we defined the material of the wheel when creating the part, we can leave the source of the properties as "Part". The mass moment of intertia about the Z-axis that was previously calculated (609.3 lb<sub>m</sub>·in<sup>2</sup>) is

shown.

It is necessary to use a consistent set of units to apply this equation. The mass properties of the wheel were calculated with lb<sub>m</sub> (pounds-mass) as the units of mass.

A pound is a measure of weight, not mass. A pound-mass is the mass of an object that weighs one pound at sea level.

To convert weight in pounds to mass, it is necessary to divide by the gravitational constant, 32.2 ft/s<sup>2</sup> or 386.4 in/s<sup>2</sup>. Since the inch is our unit of length, we will use the latter. Therefore I, the mass moment of inertia, is:

$$I = \frac{609.3 \,\text{lb} \cdot \text{in}^2}{386.4 \,\frac{\text{in}}{\text{s}^2}} = 1.577 \,\,\text{lb} \cdot \text{in} \cdot \text{s}^2$$

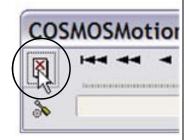
The angular acceleration  $\alpha$  must be expressed in radians per second squared:

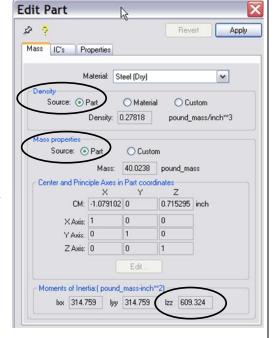
$$\alpha = \left(600 \frac{\text{deg}}{\text{s}^2}\right) \left(\frac{\pi \text{ rad}}{180 \text{ deg}}\right) = 10.47 \frac{\text{rad}}{\text{s}^2}$$

The torque can now be calculated as:

$$\Sigma M = T = I\alpha = (1.577 \text{ lb} \cdot \text{in} \cdot \text{s}^2) (10.47 \frac{\text{rad}}{\text{s}^2}) = 16.5 \text{ in} \cdot \text{lb}$$

This result agrees with the COSMOSMotion result.

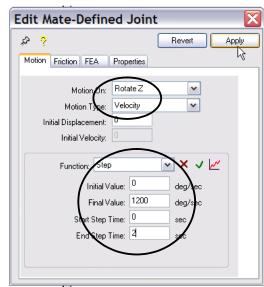




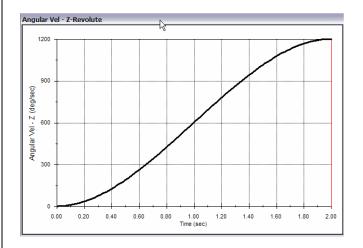
Note that the torque required to produce the constant acceleration is also constant. Therefore, the torque would need to be applied *instantaneously*, which is impossible. If our goal is to reach a constant angular velocity of 1200 deg/s (200 rpm) in 2 seconds, then we may consider a motion profile that starts with an acceleration of zero and ramps up to a maximum value and then ramps back down to zero. In this case, the torque is allowed to ramp up and down smoothly.

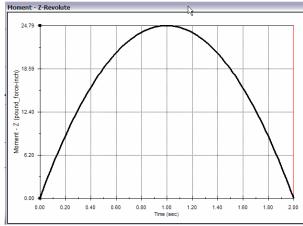
Click the calculator icon on the Simulation Panel to delete the previous results. Right-click on the Revolute joint in the Motion Model Manager and change the Motion Type to Velocity. Select a Step Function with an initial value of 0 deg/s, a final value of 1200 deg/s, a start time of 0 seconds, and an end time of 2 seconds. Click Apply, and run the simulation.

The graphs previously created are refreshed. Note that the angular velocity profile is an S-shaped curve, as the acceleration (the slope of the velocity curve) begins and ends at zero and peaks in the middle. The torque now smoothly increases to a maximum value at a time one second and smoothly decreases back to zero. Although the peak torque (24.79 in·lb) is higher than before, the smooth torque curve is



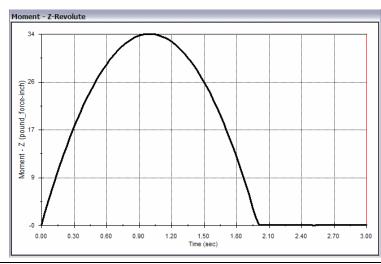
preferred. In particular, the *jerk* (rate of change of acceleration) is no longer infinite.





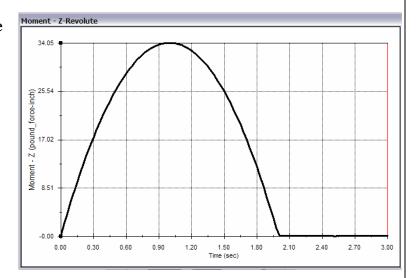
# Delete the results. Set the duration of the simulation to 3 seconds. Repeat the simulation.

Notice that the angular velocity remains at 1200 deg/s after 2 seconds. Also, the torque remains at zero. If no friction is present in the model, then maintaining a constant rotational speed requires no torque.



Return to the FeatureManager and delete the Wheel part. Insert Wheel 2, and add concentric and coincident mates as before. Switch to the Motion Model Manager, and set the properties of the revolute joint to velocity, with a step function as described above. Run the simulation.

Note that the peak torque is 34.05 in·lb, which is 37% higher than before. This increased torque is proportional to the increased moment of inertia of the new wheel.



#### Analysis of a 4-Bar Linkage

We will now analyze the motion of the 4-bar linkage shown here. We will specify a constant rotational velocity for the crank and will find the velocities and accelerations of the other links, the torque required to drive the mechanism, and forces at the pin joints.

NOTE: This analysis will not predict the stresses in the links, since the links are assumed to be rigid. However, the forces calculated can be used as inputs to finite element analysis.

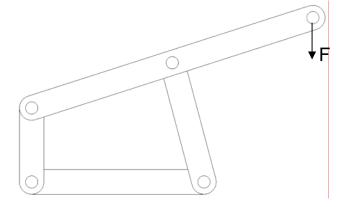
Open a new assembly. Insert the frame link, and then insert the other three links in the approximate locations shown.

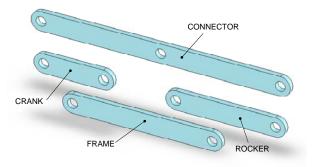
Switch to the motion model. When prompted to add the parts to grounded and moving parts in the motion

Assem1 (Defaul

model, click Yes. Open the Simulation Panel.

Throughout this tutorial, any message boxes can be deleted by selecting Dismiss.







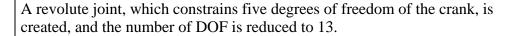
Note that there are 18 DOF, six for each of the three moving links.

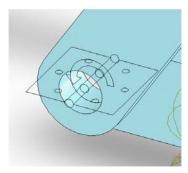
Click the calculator icon to run the simulation.

The moving links will all fall off the screen, as the motion model includes gravity.

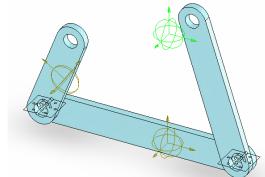
Click the calculator icon again to clear the results and reset the components.

Add a coincident mate between the back face of the crank and the front face of the frame. Add a concentric mate between the corresponding cylindrical faces of the frame and crank. Be sure to select faces and not edges; if edges are selected, then the resulting joints in the motion model may be incorrect. Close the Mate PropertyManager, and select Calculate from the Simulation Panel.

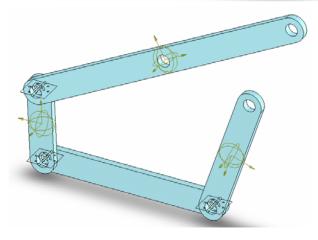




Add coincident and concentric mates between the frame and rocker, creating another revolute joint and reducing the number of DOF to 8. Move the crank and rocker to the approximate positions shown here.

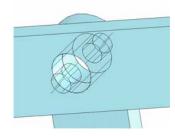


Add coincident and concentric mates between the crank and connector, creating a third revolute joint and reducing the number of DOF to 3.

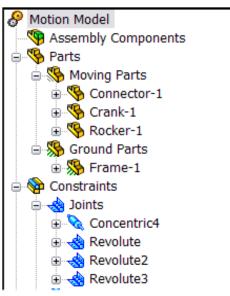


Finally, add a concentric relation between the connector and the rocker.

Although the symbol that appears on the last joint appears to be that of a cylindrical joint, in the Motion Model Manager it is identified as a concentric joint. A cylindrical joint would place redundant constraints on the model. (The revolute between the crank and

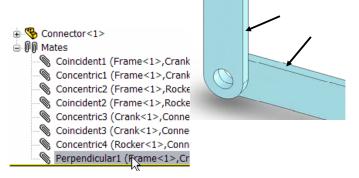


connector has already constrained the rotations about the x and y axes of the connector. Therefore, the new joint is defined to constrain only the x and y translations of the pin joint.) The Simulation Panel now shows the number of DOF to be one, which means that the mechanism can be completely controlled by driving one on the links.



To define the starting position of the mechanism, we will set the crank to be perpendicular to the frame.

Add a perpendicular mate to the faces shown here. Switch to the FeatureManager, and right-click on the perpendicular mate just created. Select Suppress.



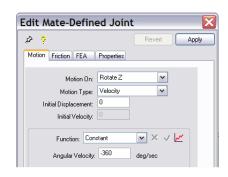
This will remove the constraint defined by the mate (and the corresponding joint in the motion model), but the orientation of the links will remain.

We will now define the motion of the crank.

Click on the plus sign next to Joints in the FeatureManager. As you click on each joint, the joint will be highlighted in green on the screen. Select the revolute joint that connects the frame link and the crank.

Right-click on the revolute joint, and choose Properties. Set the motion type as "Velocity", the function to "Constant", and the angular velocity to -360 degrees per second (60 rpm).

In COSMOSMotion, the positive direction for applied rotations is clockwise, which is the opposite from most the typical "right hand rule" sign convention. (Align the thumb of your right hand along the axis of rotation, and your fingers will curl in the positive direction of rotation.) *Velocities and accelerations from the analysis generally* 



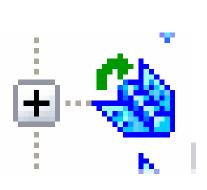
Constraints

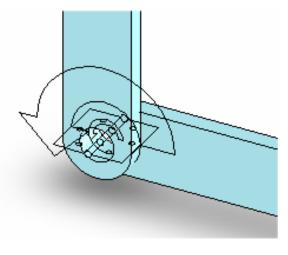
Joints

Concentric4

follow the right-hand rule convention, but extreme care should be taken in evaluating the signs.

Note that arrows appear on the joint name in the FeatureManager and on the joint itself, indicating the there is applied motion on this joint. The number of degrees of freedom is now zero.





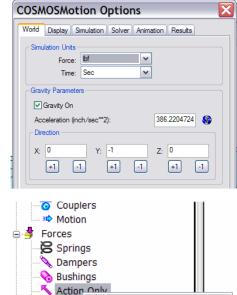
Click on the Simulation Settings button on the Simulation Panel. Under the World tab, make sure that the gravity is on, with a value of 386 in/s², with the gravity direction in the –y direction, as indicated by a -1 in Y box. (The gravitational constant can be reset by clicking the icon next to the numerical value.)



Under the Simulation tab, set the duration to one second and the number of frames to 100.

Before running the simulation, we will add a force to the open hole of the connector.

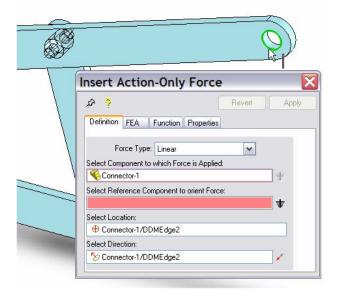
Right-click on Action-Only under the Forces and select Add Action-Only Force.



Add Action-Only Force

Add Action-Only Moment

Select the edge of the open hole on the connector as the component to which the force will be applied (by selecting the hole, both the component and the location of the force will be selected).

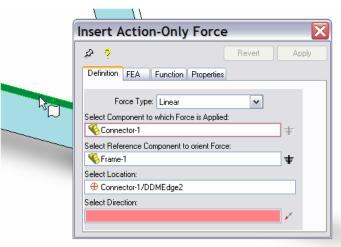


Action

L Trace Path

- ■ Results

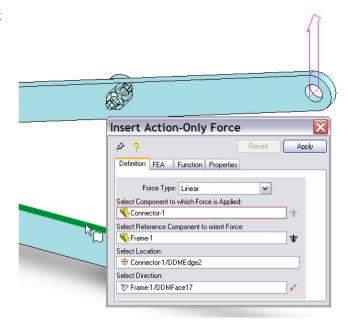
Select the ground link as the referencedirection link.



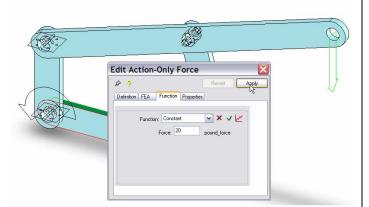
In the Select Direction box, delete the entry in the box. With the box highlighted in pink, select the top face of the ground link. The direction of the force will be perpendicular to this face.

The force is now shown acting upwards. Click on the arrows to change the direction.





Select the Function tab and set the force to 20 pounds, and click Apply.



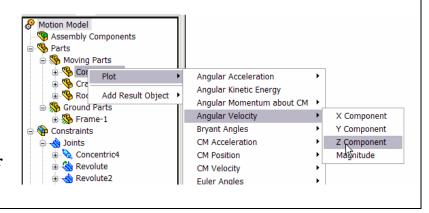
Check the mass properties of each of the moving parts by right-clicking on each and selecting Properties.

If you defined the material of each part as steel, then the density box should display about 0.28 pounds per cubic inch. If you did not define the properties, then the value defaults to the density of water (0.036 pounds per cubic inch). You may override the part-defined properties by selecting a new material here or by entering a density value.

# Run the simulation by clicking the calculator icon.

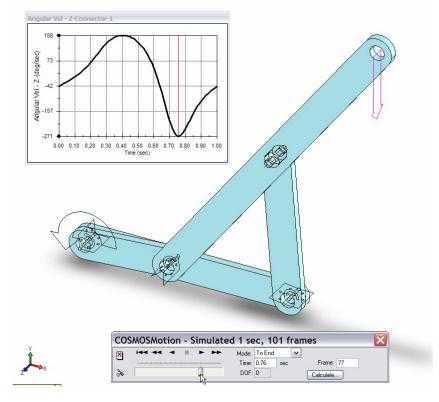
Velocities, accelerations, forces, and moments can now be plotted.

To view the angular velocity of the connector, right-click on the connector under Moving Parts, pick Plot-Angular Velocity-Z Component.



By moving the slider bar on the Simulation panel, you can find the approximate position of the mechanism at which the magnitude of the angular velocity of the connector is maximized.

To remove the graph, right-click on it and select delete.

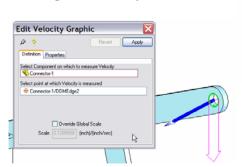


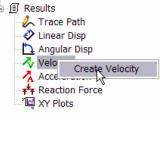
You can add graphics showing the directions and relative magnitudes of the velocities and accelerations of any point.

Under Results, right-click Velocity and select Create Velocity. Click on the edge of the open hole, and an arrow showing the velocity will be

added.

Repeat with Acceleration to add an acceleration graphic.





As you move the slider bar on the Simulation Panel, the velocity and acceleration arrows will change direction and length.

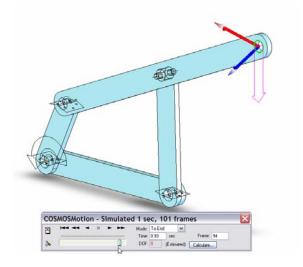


Chart Properties...

Copy Clipboard

Export CSV

Save As

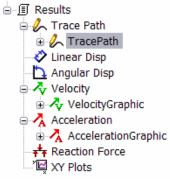
Hide Delete

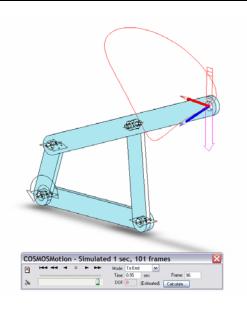
You can also add a trace path, which shows the position of a point throughout the simulation.

Right-click Trace Path, and select Create Trace Path. Select the edge of the open hole as the location.

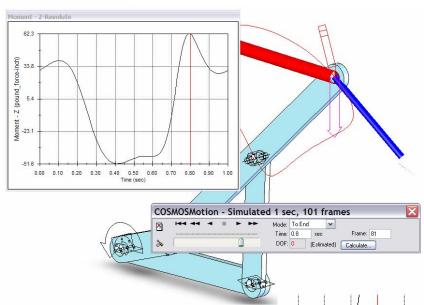
The trace path will be displayed, with a pencil icon showing the current position of the trace point.

Each of these graphic elements is stored in the Results section, from where it can be edited or deleted.





To display the torque required to drive the crank at 60 rpm, right-click on the revolute joint for which the motion was applied, and select Plot-Rotary Motion Generator-Z Moment. At the position shown here, the maximum torque of 62.3 in-lb is required to maintain the velocity of the crank.



To save the actual data displayed on the graph, right-click on the graph and select Export CSV. This will create a data file that can be opened in Excel.

As we see here, the torque is about 30 in-lb at the beginning of the simulation.

	A	В				
1	Moment - Z-Revolute					
2	Time (sec)	Moment - Z (pound_force-inch)				
3	0	29.963				
4	0.01	30.995				
5	0.02	32.096				
6	0.03	33.226				
7	0.04	34.346				
8	0.05	35.417				
9	0.06	36.399				
10	0.07	37.254				
11	0.08	37.942				
12	0.09	38.423				
13	0.1	38.660				
·	2 4 4	00.044				

Since the rotational speed is fairly low, you may assume that the inertial effects of the accelerating links are small compared to the applied 20-pound load. Confirm this by changing the rotational velocity.

Delete the results by clicking on the calculator icon and change the rotational velocity of the crank by right-clicking on the revolute and selecting Properties. Change the velocity to –36 degrees per second (6 rpm). Change the duration of the simulation to 10 seconds and run the analysis.

Note that the maximum torque is only slightly less than for the previous analysis, about 61 in-lb. Further evidence that the inertial effects are low can be seen by conducting a static force analysis, as is shown in the hand calculations on pages 19 and 20. Ignoring both the accelerations of the members and the member weights, it is seen that a torque of 29.4 in-lb is required for static equilibrium of the mechanism when the members are in their starting positions.

Delete the analysis results. From the Simulation Panel, choose the Simulation settings and turn gravity off. Run the analysis, and save the torque results to a CSV file.

This result for the torque at time =0 agrees with that calculated in the hand analysis. An analysis in which the inertial forces are small is sometimes referred to as a "quasi-static" analysis. Although a static analysis produces good results if inertial force are low, the advantage of our computer solution is that a complete revolution has been considered. The hand calculations only apply to a single point in time, which of course may not be the time at which the forces are maximized.

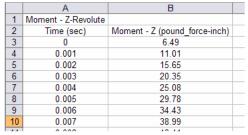
	Α	В				
1	Moment - Z-Revolute					
2	Time (sec)	Moment - Z (pound_force-inch)				
3	0	29.435				
4	0.1	30.290				
5	0.2	31.212				
6	0.3	32.164				
7	0.4	33.107				
8	0.5	34.003				
9	0.6	34.815				
10	0.7	35.504				
11	0.8	36.034				
12	0.9	36.367				

Delete the results by clicking on the calculator icon and change the rotational velocity of the crank by right-clicking on the revolute and selecting Properties. Change the velocity to -3600 degrees per second (600 rpm). Change the duration of the simulation to 0.10 seconds, turn on the gravity, and run the analysis.

The maximum torque is now found to be about 270 in-lb. At this higher rotational speed, the inertial effects of the members now make a large contribution to the solution. By saving and viewing the .CSV file, we see that the value of torque at the beginning position (crank is vertical) is 6.49 in-lb. This value is verified in the dynamic analysis hand calculations beginning on page 21.

Simulation results can be exported as Excel spreadsheets. For example, we can export force on joint between the crank and connector (Revolute3).

From the menu, select Motion-Export Results-To Spreadsheet. For the Element with Results, select the Revolute3 Joint. For the Result Characteristic, select Force. For Components, select X.





We will plot both components of force (the Z-direction force is zero) and the magnitude on a single graph.

Click on Add 1 Curve and select Revolute3-Force-Y.

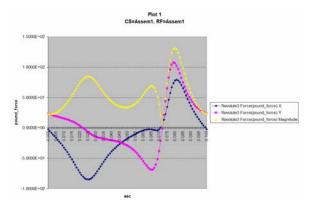
Click on Add 1 Curve and select Revolute3-Force-Magnitude.

Now select Add 1 Curve and OK.

Excel will be opened, and the graph displayed. The actual numerical data is stored on Sheet 1 of the spreadsheet.

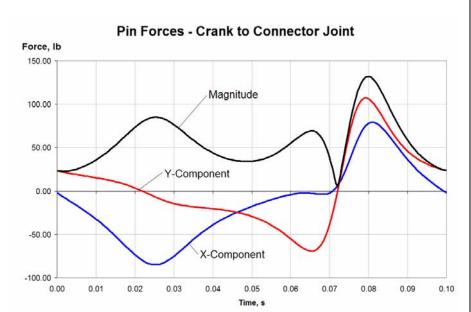
Note that the value of the pin forces at time = 0 (X-component = -2.16 pounds, Y-component = 23.55 pounds) agree with the hand calculation results for joint "B" on page 30.





# Edit the graph in Excel to make it look the way you want.

The graph type is a Line graph. You may want to right click on the graph and change the graph type to XY plot to have more control of the graph's appearance.

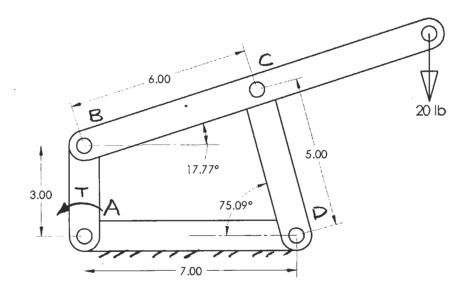


Video files are easy to create.

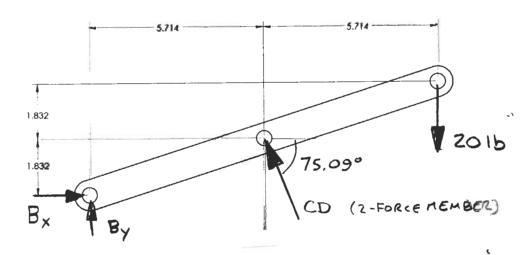
#### Select Motion-Export Results-to AVI Movie. Set the path to which the file will be saved, and OK.

Note that the Simulation Panel and any results windows will appear in the movie if they are open in the model area. To play the movie, go to the directory where you stored it and double-click on the file name.

### FORCE ANALYSIS - STATIC CASE



#### FREE BODY DIAGRAM OF CONNECTOR:



$$\Sigma M_B = (5.714 \text{ m.}) CD \text{ sin}(75.09°) + (1.832 \text{ m.}) CD \text{ cou}(75.09°)  $-2(5.714 \text{ m.})(20 \text{ lb}) = 0$ 
 $CD = 38.14 \text{ lb}$$$

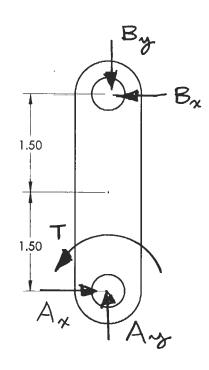
$$\Sigma F_{x} = B_{x} - (38.1416) cov(75.09°) = 0$$

$$B_{x} = 9.813 \text{ lb}$$

$$\Sigma F_{y} = B_{y} + (38.1416) sin(75.09°) - 2016 = 0$$

$$B_{y} = -16.86 \text{ lb}$$

#### FREE BODY DIAGRAM OF CRANK



$$\Sigma M_A = (3in) B_X + T$$

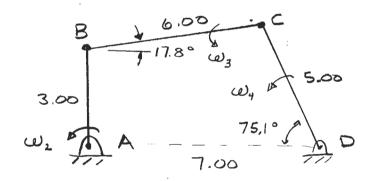
$$= 0$$

$$T = -(3in)(9.81316)$$

$$T = -29.44 in.16$$

NOTE THAT COSMOSMOTION RESULT IS POSITIVE.

# VELOCITY ANALYSIS



$$N_{BX} = 3\omega_{2} = 188.5 \%$$

$$N_{BX} = -188.5$$

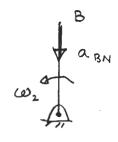
$$N_{BY} = 0$$

$$N_{c} = 5 \omega_{4}$$
  
 $N_{bx} = -N_{B} \sin(75.1^{\circ})$   
 $= -4.832 \omega_{4}$   
 $N_{by} = -N_{B} \cos(75.1^{\circ})$   
 $= -1.286 \omega_{4}$ 

$$N_{c/8} = 6 \omega_3$$
 $N_{c/8} = -N_{6} \sin(17.8^{\circ})$ 
 $= -1.834 \omega_3$ 
 $N_{c/8} = N_{48} \cos(17.8^{\circ})$ 
 $= 5.713 \omega_3$ 

$$\chi$$
: -4.832  $\omega_4 = -188.5 - 1.834 \omega_3$ 

# ACCELERATION ANALYSIS



$$a_{BN} = \omega^{2} \Gamma$$

$$= (62.83^{rad})^{2} (3_{10})$$

$$= (11,840^{10})^{2}$$

$$a_{CN} = (0)^{2}r$$

$$= (35.94^{rad/3})^{2} (51n)$$

$$= (6458^{11/3}2)$$

$$= 6458^{11/3}2$$

$$= 6458^{11/3}2$$

$$= 6458^{11/3}2$$

$$Q_{CX} = 6458 cav(75.1°) - 5 dy si(75.1°)$$

$$= 1661 - 4.832 dy$$

$$Q_{CY} = -6458 sin(75.1°) - 5 dy cav(75.1°)$$

$$= -6241 - 1.286 dy$$

$$a_{c/6N} = (\omega^{2}r)$$

$$= (8.094 ^{md/s})^{2} (6n)$$

$$= 393.1 ^{11/s}z$$

$$a_{c/BT} = \alpha r = 6\alpha_{3}$$

$$\alpha_{c/8} = -393.1 \text{ cm}(17.8^{\circ}) - 6\alpha_3 \text{ si}(17.8^{\circ})$$

$$= -374.3 - 1.834 \alpha_3$$

$$a_{c/B_{7}} = -393.1 \text{ sin} (17.8^{\circ}) + 6 \times_{3} \text{ cos} (17.8^{\circ})$$

$$= -120.2 + 5.713 \times_{3}$$

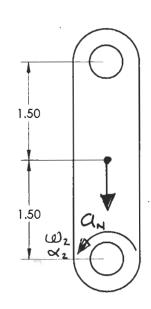
OR

$$\begin{bmatrix} 1.834 & -4.832 \\ -5.713 & -1.286 \end{bmatrix} \begin{pmatrix} \alpha_3 \\ \alpha_4 \end{pmatrix} = \begin{pmatrix} -2035 \\ -5719 \end{pmatrix}$$

SOLUTION:

# ACCELERATIONS OF CG'S OF MEMBERS

#### CRANK:

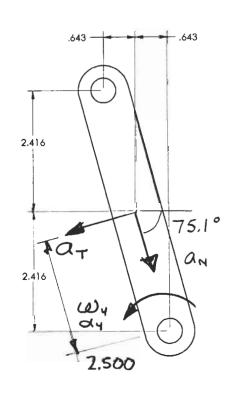


$$\omega_z = 62.83 \text{ rad/s}$$
 $\alpha_z = 0$ 
 $\alpha_N = (\omega^z r = (67.83)(1.5)$ 

$$a_N = \omega^2 r = (67.83)(1.5)$$

$$= 5921 \% s^2$$

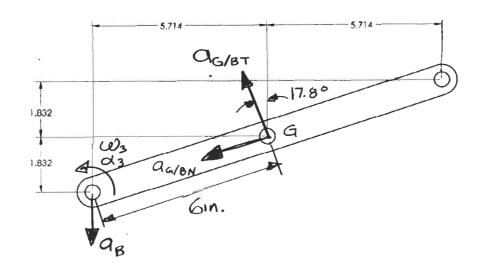
# ROCKER:



$$\omega_{4} = 35.94^{\text{red/s}}$$
 $\omega_{4} = 738.0^{\text{red/s}}$ 
 $\omega_{4} = 738.0^{\text{red/s}}$ 
 $\omega_{N} = \omega^{2}r = (35.94)^{2}(2.5) = 3229$ 
 $\omega_{7} = \omega_{7} = 738(2.5) = 1845$ 

$$a_x = -952.7 \frac{11}{5^2}$$
  
 $a_y = -3595 \frac{11}{5^2}$ 

#### CONNECTOR:



$$\vec{a}_{6} = \vec{a}_{8} + \vec{a}_{6/8}$$

$$\vec{a}_{3} = 11840 \%^{2} + \frac{1}{3}$$

$$\vec{a}_{6/3N} = \omega^{2}r = (-8.094)^{2}(6) = 393.1 \%^{2}$$

$$\vec{a}_{6/3N} = \vec{a}_{7} = (-8.094)^{2}(6) = 5009 \%^{2}$$

$$\vec{a}_{6/3N} = \vec{a}_{7} = (-8.094)^{2}(6) = 5009 \%^{2}$$

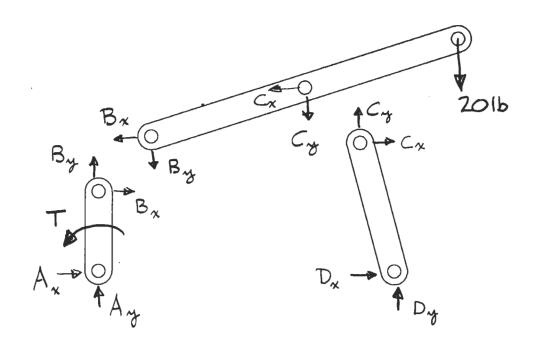
$$\vec{a}_{6/3N} = \vec{a}_{7} = (-8.094)^{2}(6) = 5009 \%^{2}$$

$$\vec{a}_{6/3N} = \vec{a}_{7} = (-8.094)^{2}(6) = 393.1 \%^{2}$$

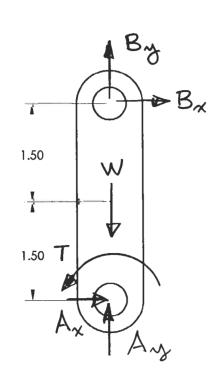
$$\vec{a}_{6/3N} = (-8.094)^{2}(6) = 393.1 \%^{2}$$

NOTE: AN ALTERNATE METHOD OF FIND INC THIS ACCELERATION IS TO NOTE THAT THE CG COINCIDES WITH POINT C, WHICH IS ALSO A POINT ON THE ROCKER. SINCE C IS TWICE AS FACE FROM THE PIVOT POINT AS COMPARED TO THE CG OF THE ROCKER, ITS ACCELERATION IS ZX THAT OF THE CG.

# DYNAMIC FORCE ANALYSIS

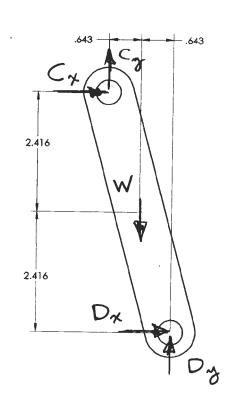


#### CRANK:



W = 0.2359 lb  $M = 0.2359 \text{ lb}(386.4 \frac{11}{51}) = 0.0006 \text{ los} \frac{10.52}{10}$   $I = 0.276 \text{ lb·in}^2/(386.4 \frac{11}{51})$   $= 0.0007 \text{ l45 lb·s}^2 \cdot \text{ln}$  d = 0  $a_x = 0$   $a_y = -592 \text{ lings}^2$   $\Sigma F_x = A_x + B_x = ma_x = 0$   $A_x + B_x = 0$  = 0.006 los(-592 l)  $A_x + B_y = -3.379 \text{ lb}(2)$   $\Delta M_x + B_y = -3.379 \text{ lb}(2)$ 

# ROCKER:



$$W = 0.3750 | b$$

$$M = 0.3750 | b / (386.4 \% 2)$$

$$= 0.0009705 | b \cdot 5 \% n$$

$$T = 0.9880 | b \cdot m^2 / (386.4 \%)$$

$$= 0.0002557 | b \cdot 5^2 \cdot m$$

$$Q = 738.0 | rad \% 2$$

$$Q_{\chi} = -952.7 | r\%_5^2$$

$$Q_{\chi} = -3595 | r\%_5^2$$

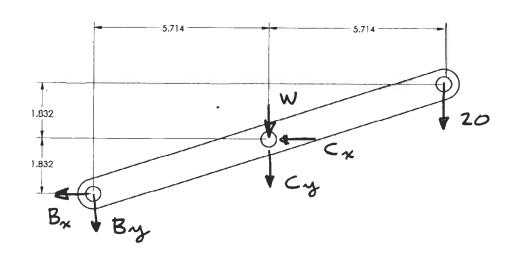
$$\Sigma F_{x} = C_{x} + D_{x} = ma_{x} = .0009705(-952.7)$$

$$C_{x} + D_{x} = -.9246 \quad \textcircled{1}$$

$$\Sigma F_{g} = C_{g} + D_{g} - .3750 = ma_{y} = .0009705 (-3595)$$

$$C_{g} + D_{g} = -3.114$$

#### CONNECTOR :



 $W = 0.8482 \, lb \quad m = .8482/(386.4 \, \%_c) = 0.002195 \, \frac{lb \cdot 5^2}{m}$   $T = 11.21 \, lb \cdot ln^2/(386.4 \, \%_c) = 0.0290 \, lb \cdot 5^2 \cdot ln$   $Q = 834.9 \, rad_{5^2} \quad \alpha_x = -1905 \, \%_c \quad \alpha_y = -7190 \, \%_c^2$ 

$$\Sigma F_{x} = -B_{x} - C_{x} = ma_{x} = .002195 (-1905)$$

$$-B_{x} - C_{x} = -4.181$$

EFy = -By - Cy -.8482 - Zo = May =.002195 (-7190)

EMG= -1.832 Bx + 5.714 By - 5.714 (20) = IX = .0290 (834.9)

# No. 937 811E Engineer's Computation Pad STAEDTLER®

# SOLUTION OF SIMULTANEOUS EQUATIONS:

_												
1	.0	1	0	0	0	0	0	0	$A_x$		0	)
1.5	0	1.5	0	0.	0	0	0	0	$A_{y}$		-3.379	
1.5	0	-1.5	0	0	0	0	0	1	$B_x$		0	
0	0	0	0	1	0	1	0	0	$B_{y}$		9246	
0	0	0	0	0	1	0	1	0	$\left\{ C_{x}\right\}$	· = ·	-3.114	}
0	0	0	0	-2.416	6432	2.416	.6432	0	$C_{y}$		1.887	
0	0	-1	0	-1	0	0	0	0	$D_x$		-4.181	
0	0	0	-1	0	-1	0	0	0	$D_{y}$		5.066	
0	0	-1.832	5.714	0	0	0	0	0	$\left[\begin{array}{c} T \end{array}\right]$		138.5	

#### SOLUTION:

PIN FORCES:

$$D_{x} = -7.2716$$
 $D_{y} = 25.516$ 

TORQUE:

.. TORQUE PIRECTION IS CW